Hodge theory of stratified varieties
Lecture notes for 18.157, Spring 1997

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Introduction

In these lectures I plan to describe the Hodge theory for a certain class of spaces which includes stratified varieties; these general spaces are sometimes called *pseudomanifolds*[1]. Most of the new material here represents joint work with Rafe Mazzeo.

[1]The definition I take is a little wider than the usual one, so as to include manifolds with boundary and even corners.