

Errata and Addenda in S. Helgason: The Radon Transform 2<sup>nd</sup> Edition (First Printing)

These have been entered in the downloadable version.

Page and line in $\begin{cases} \text{above} \\ \text{below} \end{cases}$	Instead of:	Read:
3 <sup>2</sup>	omit “ $\varphi$ on $\mathbb{P} \dots$ , functions ”	
5 <sub>10</sub>	$R^n$	$\mathbb{P}^n$
11 <sub>12</sub>	$\pi^{-\frac{1}{2}}$	$\pi^{\frac{1}{2}}$
12 <sup>4</sup>	(i)	(ii)
16 <sub>11</sub>	$dk)$	$)dk$
17 <sub>14</sub>	replaced by $f(x) = 0( x ^{-n})$	dropped
17 <sub>13</sub>	with	for all lines with
25 <sub>18</sub>	$f * \varphi$	$f \times \varphi$
26 <sub>14</sub>	$\neq$	$=$
26 <sup>12</sup>	$\text{supp}(\widehat{S}) \subset S_R(0)$	$\text{supp}(S) \subset S_R(0)$
28 <sup>8</sup>	$\psi_n$	$\psi$
34 <sup>9</sup>	(63)	(64)
35 <sup>3</sup>	(68)	(69)
35 <sup>7</sup>	$i, j$	$i \neq j$
35 <sup>6</sup> , 35 <sub>1</sub> , 36 <sup>2</sup> , 36 <sup>9</sup>	$\partial_{2,1}, \partial_{2,d+1}$	$\partial_{1,1}, \partial_{1,d+1}$
36 <sup>9</sup> , 36 <sup>12</sup> , 36 <sup>14</sup>	$\partial_{2,n}$	$\partial_{1,n}$
39 <sup>7</sup>	$-\xi_1 + \xi_2 - \eta_1$	$-\xi_1 + \xi_2 + \eta_1$
40 <sup>7</sup>	$z^2$	$(z^2 + 1)$
40 <sub>3</sub>	$xy$	$xy^2$
42 <sub>5</sub>	$f_1(0)$	$f_1(x)$
42 <sub>2</sub>	$h(\langle x, w \rangle)$	$h(\langle x, w \rangle + t)$

Page and line in $\begin{cases} \text{above} \\ \text{below} \end{cases}$	Instead of:	Read:
44 <sup>9</sup>	$w_{i_k}$	$w_{i_k} dw$
44 <sub>5</sub>	$\tilde{f}$	$\tilde{f}_1$
58 <sup>11</sup>	$o$	$c$
62 <sup>4</sup>	$(\lambda(D)f)^\checkmark$	$(\lambda(D)f)^\wedge$
67 <sup>4</sup>	cosh	coth
69 <sup>3</sup>	$k'a_{t'}, n'a_t N \cdot 0$	$k'a_{t'} n'a_t N \cdot 0$
69 <sup>12</sup>	-2	-1
69 <sub>6</sub>	$ch s$	$ch^3 s$
97 <sup>5</sup>	a circle	two circles.
97 <sup>7</sup>	“a circular arc”	“a pair of circular arcs”
98	$k - 1$	$(k - 1)!$ .
101 <sup>10</sup> , 101 <sub>2</sub>	$f \times \tau$	$\pi^{-1} f \times \tau$
101 <sub>7</sub>	$-4\pi^2$	$-4\pi$
103 <sup>3</sup> , 103 <sup>12</sup>	$(4n + 1) \sum_0^\infty$	$\sum_0^\infty (4n + 1)$
119 <sup>6</sup>	formula	formula $f = Q(L)((\tilde{f})^\checkmark)$ . Here $Q$
153 <sub>4</sub>	sequences	positive sequences
153 <sub>15</sub>	$n + 1$	$-(n + 1)$
153 <sup>5</sup>	Absolute value signs missing	
154 – 155	In equations (20), (23), (24) 1 should be replaced by 2	
156 <sub>2</sub>	(1)	(25)
156 <sub>5</sub>	Interchange $P_1$ and $G_1$	
167 <sup>13</sup>	(60)	(61)
180 <sup>12</sup>	397	394

44<sub>4</sub> Here one should use the following remark: If  $\varphi(\lambda)$  is even, holomorphic on  $\mathbb{C}$  and satisfies the exponential type estimate (13) in Theorem 3.3, Ch. V, then the same holds for the function  $\Phi$  on  $\mathbb{C}^n$  given by  $\Phi(\zeta) =$

$\Phi(\zeta_1, \dots, \zeta_n) = \varphi(\lambda)$  where  $\lambda^2 = \zeta_1^2 + \dots + \zeta_n^2$ . To see this put

$$\lambda = \mu + iv, \quad \zeta = \xi + i\eta \quad \mu, \nu \in \mathbf{R}, \quad \xi, \eta \in \mathbf{R}^n.$$

Then

$$\mu^2 - \nu^2 = |\xi|^2 - |\eta|^2, \quad \mu^2 \nu^2 = (\xi \cdot \eta)^2,$$

so

$$|\lambda|^4 = (|\xi|^2 - |\eta|^2)^2 + 4(\xi \cdot \eta)^2$$

and

$$2|\operatorname{Im} \lambda|^2 = |\eta|^2 - |\xi|^2 + [(|\xi|^2 - |\eta|^2)^2 + 4(\xi \cdot \eta)^2]^{1/2}.$$

Since  $|(\xi \cdot \eta)| \leq |\xi| |\eta|$  this implies  $|\operatorname{Im} \lambda| \leq |\eta|$  so the estimate (13) follows for  $\Phi$ .

45<sub>1</sub> Note that Part (ii) can also be stated: The solution is outgoing (incoming) if and only if

$$\int_{\pi} f_0 = \int_{H_{\pi}} f_1 \quad \left( \int_{\pi} f_0 = - \int_{H_{\pi}} f_1 \right)$$

for an arbitrary hyperplane  $\pi$  ( $0 \notin \pi$ )  $H_{\pi}$  being the halfspace with boundary  $\pi$  which does not contain 0.

58<sup>11</sup> The subscripts 0 should be  $c$ .

102<sup>4</sup> The function  $\tau$  is only locally integrable but not integrable. However for  $\lambda$  real  $\tau \varphi_{\lambda}$  is integrable and (62) holds by virtue of the proof of (53), p. 100.

102<sub>11</sub> The implication (62) & (63)  $\Rightarrow$  (60) is justified as follows. Using the decomposition  $\tau = \varphi\tau + (1 - \varphi)\tau$  where  $\varphi$  is the characteristic function of a ball  $B(0)$  we see that  $f \times \tau \in L^2(X)$  for  $f \in \mathcal{D}^b(X)$ . Since  $\sigma \in L^1(X)$  we have  $f \times \tau \times \sigma \in L^2(X)$ . Now (60) follows since by the Plancherel theorem the spherical transform is injective on  $L^2$ .

155<sup>3</sup> From formula (24) below for  $j = 0$  and  $j = 1$ , it is clear that sequences  $\delta_1, \delta_2, \dots, M_1, M_2, \dots$  ( $\delta_i > 0, M_1 > 0$ ) exist such that (3) holds for  $j = 0, j = 1$ . Fix the  $\delta_1$  and  $M_1$ . Then the idea is to shrink  $\delta_2, \delta_3 \dots$  and  $1/M_2, 1/M_3, \dots$  so that by the argument below, (3) holds for  $j = 2$ , etc.

167<sup>13</sup> (60) should be (61). It should also be observed as a result of (39) that if  $f(x) = O(|x|^{-N})$  then  $I^{\lambda}f(x)$  is holomorphic near  $\lambda = 0$  and  $I^0 = f$ .

168<sub>11</sub> The idea of a proof of this nature involving a contour like  $\Gamma_m$  appears already in Ehrenpreis [1956], although not correctly carried out in details.