MIT Dept. of Mathematics Benjamin Seibold

## 18.086 spring 2008

Bonus Exercise Sheet

Out Wed 03/19/08

Due Wed 04/23/08

**Exercise** Consider the Matlab program mit18086\_navierstokes.m from the CSE web page, which solves the incompressible, viscous flow in a lid driven cavity.

- 1. Extend the program to allow one hole in the geometry. Let the hole be a rectangle, and allow the position and size of the hole to be chosen by the user. Preserve as much as possible of the vectorized structure, and try to create brief code.
- 2. Allow further to choose inflow and outflow boundaries.
- 3. Use your program to compute the flow around an obstacle. Let the horizonal walls be no-slip walls. On the left wall prescribe a parabolic inflow profile. On the right wall prescribe outflow boundary conditions. All four boundaries of the hole shall be no-slip walls. Initially, the whole fluid shall be at rest.
- 4. Use your code to show the transition to turbulence by running it for various Reynolds numbers. Produce videos of your simulation.

## **Rules:**

- This problem set is a bonus. It is worth 15 bonus points for your homework score.
- The whole class submits *one* solution. At most one solution. Not more. **One**! Everybody receives the bonus points granted.
- If you make the obstacle a circle, you can get 20 bonus points instead of 15.